Underspecified (Embedded) Tense Semantics

Abstract

In this paper, we provide a novel, compositional underspecification account of past tense semantics, which explains the systematic availability of both backward-shifted and simultaneous readings in past-under-past embeddings—a phenomenon commonly referred to as Sequence of Tense (SoT)—without assuming ambiguity at the level of LF. We show that this approach fairs at least equally well as other existing SoT analyses in terms of the range of data it can account for, and that it has additional advantages over them as well, such as retaining the one-to-one mapping between past tense form and past tense meaning.

We move on to demonstrate that the proposed underspecification account is straightforwardly extendable to present tense embeddings. A crucial component of this proposal is that the double-access reading actually contributes the present tense's inherent meaning.

1 Introduction

Typically, past tense morphology systematically marks that the event expressed by the verb or predicate of a sentence is located prior to the time of utterance (1), whereas present tense morphology denotes that the sentence's event time is ongoing at the time of utterance (2):

- (1) Mary was ill (*now/last year/*next year).
- (2) Mary is ill (now/*last year/*next year).

Nevertheless, it is well-established in the literature that for either of the two tenses this is not always the case. Across different matrix embeddings, the meaning of their tense morphemes appears to vary: In past-under-past embeddings, the contribution of embedded past tense morphology may appear to be vacuous (cf. Section 1.1); The semantic contribution of present tense morphology sometimes appears to anchor an event to some evaluation time rather than just anchoring it to the utterance time (cf. Section 1.2). In this article, we propose a novel syntactic-semantic account for past and present tense that can explain the full range of their behavior while retaining a one-to-one mapping between tense form and meaning. Before outlining the structure of the argument, let us briefly recapitulate why embedded tenses pose such an interesting and important puzzle to solve.

1.1 The embedded past tense puzzle

It has long been known that sentences in which a past tense is embedded under a matrix past have two readings: a simultaneous [sim] and a backward-shifted [b-s] one, where the former constitutes the most salient interpretation.

(3) John said Mary was ill.

- a. John, at some t' < utterance time, t_u : "Mary is ill." [sim]
- b. John, at some $t' < t_u$: "Mary was ill." [b-s]

The availability of the sim reading for past-under-past constructions is commonly referred to as Sequence of Tense (SoT) and has been a prevalent topic of research for an extensive period of time already since Curme (1931); Jespersen (1931). One reason for the continuing interest is that, intuitively, there are two ways to think about past tense, and each of them fails to predict the two-fold meaning distinction observed in (3). Leaving the various implementation variants on the market aside for now, the puzzle boils down to the following:

Under an *absolute* view on past tense, each instance of past tense is taken to place the event time of the predicate it scopes over prior to the sentence's utterance time (cf., e.g., Reichenbach, 1947; Prior, 1967; Comrie, 1985; Declerck, 1995, 2015).

(4)
$$\llbracket PAST_{absol.} \rrbracket = \lambda P. \exists t' < t_u \& P(t')$$

In clauses in which a past tense morpheme is embedded under a matrix past, two such prior-to- t_u relations are established, but their internal order is not further specified.

(5) John say-PAST Mary be-PAST ill
$$\exists t_1 < \underline{t_u} \& say(t_1) \qquad \exists t_2 < \underline{t_u} \& be-ill(t_2)$$

Such a view correctly predicts the availability of the sim and the b-s readings for past-underpast sentences (i.e., the temporal orderings $t^2 < t^1 < t_u$ and $t^2 = t^1 < t_u$, respectively). At the same time, however, it also, incorrectly, predicts a forward-shifted [f-s] interpretation to be available, falsely supporting the following paraphrase for (3). As a result, a purely absolute theory of past tense cannot provide a final answer to the puzzle.

(6) John, at some $t < t_u$: "Mary will be ill." [f-s] (temporal ordering: $t^1 < t^2 < t_u$)

The second intuitive way to look at past tense is to regard it as a *relative* tense. Under such a view, each instance of past tense is assumed to place the event time of the predicate it scopes over prior to the predicate's evaluation time, which is provided by its closest ccommanding tense, or, in the absence of such a tense, the utterance time (cf., e.g., Prior, 1967).

(7) a.
$$\llbracket PAST_{rel.} \rrbracket = \lambda P. \lambda t^*. \exists t' < t^* \& P(t')$$

b. John say-PAST Mary be-PAST ill.
 $\exists t_1 < t_u \& say(t_1)$ $\exists t_2 < \underline{t_1} \& be-ill(t_2)$

In contrast to an absolute view on past tense, adopting a relative view correctly rules out a f-s interpretation of (3), since the matrix tense provides the evaluation time of the embedded tense. At the same time, however, such a proposal fails to predict the availability of the sim reading. The only reading it, correctly, predicts is the b-s one. Hence, neither of the two intuitive views on past tense explains the systematic two-fold meaning distinction of English past-under-past constructions.

To solve this problem, it has become received wisdom in most SoT literature that there exists some mechanism by means of which the embedded past tense may lose its semantic contribution in SoT contexts. Implementations of this insight vary, among others, from the assumption of a void tense in SoT-languages (Partee, 1973; Heim, 1994; Kratzer, 1998), to a past tense which is, in fact, a present-in-disguise (Ross, 1989; Abusch, 1988, 1997), an optional tense deletion mechanism constrained by syntax (Ogihara, 1995; Stowell, 1995, 2007), and hybrid approaches (Kusumoto, 1999; von Stechow, 2009; von Fintel & Heim, 2016). Irrespective of the different manners of implementation, however, an assumption shared by all of these proposals is Logical Form (LF)-ambiguity between the sim and bs reading. A notable exception to this assumption is provided by pragmatic approaches such as Altshuler (2016) and Altshuler and Schwarzschild (2012) that explore the presence or absence of cessation implicatures (discussed more extensively in Section 2.4.2). The assumption that past-under-past embeddings are ambiguous is also what we challenge in this paper. Nevertheless, instead of providing a pragmatic solution to the SoT problem, we argue that past tense is semantically *underspecified* and therefore compatible with both simand b-s readings, though crucially not with f-s readings.

1.2 The embedded present tense puzzle

A similar puzzle to the one presented for embedded past tense morphology can be observed for embedded present tense morphology: Present tense, too, can be interpreted in one of two different ways, depending on the matrix environment (cf. (8)). In (8a), an instance of present-tense morphology is embedded under a future-shifted matrix tense. This setting leads to a simultaneous [sim] interpretation of the present-tensed complement clause; i.e., one in which the time of Mary's illness is understood to include the time of John's saying event—which lies in the strict future of t_u —but not necessarily the utterance time t_u itself. The example in (8a) can therefore be feasibly paraphrased as follows: John, at some t later than t_u : "Mary is ill (now)." In (8b), by contrast, in which present tense morphology is embedded under a past-tensed matrix verb, the present tense is interpreted as fulfilling a different, dual role: It anchors the time of Mary's illness to both the utterance time and the time of John's saying, i.e., its evaluation time. As a result, (8b) is interpreted to be true if and only if the time interval at which the state Mary is ill holds includes both t_u and some time t prior to t_u , where t denotes the time of John's saying event. Such a reading of embedded present tense morphology is commonly referred to as a double-access [d-a] reading.

As with past tense, the established two-way meaning distinction of present tense in different environments poses a puzzle to traditional relative/absolute views on tense. A relative view on present tense predicts that each instance of present tense morphology includes its respective evaluation time; an absolute view on present tense tense proposes that present tense morphology always establishes an inclusion relation with respect to t_u (cf. Prior, 1967; Comrie, 1985; Declerck, 1995, 2015). The above data show that neither view can capture the full meaning of present tense: Whereas (8a) provides evidence for a relative and not an absolute view on present tense—as no reference to t_u is made—the example in (8b) refutes such a view: When embedded under a past matrix verb, present tense always makes reference to t_u in addition to its evaluation time. Hence, neither the relative nor an absolute view of present tense readily explains the attested readings, proving that present tense meaning should be more complex. Again, the leading intuition in the literature is that the respective embedded present tense meanings should be derived on the basis of different LF structures; one in which the tense contribution is deleted, leading to the sim interpretation, and one where it is not, yielding a d-a reading.

Even though the ambiguity of past tense morphology has received a lot of attention in the literature, the present tense morphology-counterpart of the puzzle seems to have been discussed less extensively so far. This might be due to the fact that, *prima facie*, the cases of past- and present tense morphology-ambiguity do not seem directly related, as the twoway meaning distinction of the former reveals itself within a sentence, whereas the two-way meaning distinction of the latter only reveals itself across different embedding contexts. Nevertheless, a closer inspection shows that they can be analyzed in a parallel manner. Such a unified treatment should be able to capture the meaning distribution of both past and present tense and, thus, incorporate an absolute as well as a relative meaning component. That is indeed what we will provide in this paper.

1.3 Outline of the paper

The paper is structured as follows: In Section 2, we propose a past tense semantics that is underspecified between a simple past tense and past perfect meaning. To do so, we disentangle the different meaning components of past tense via outsourcing its absolute past meaning into a structurally high, covert past operator (Op-PAST) while encoding a relative non-future meaning into the past tense morpheme (-ed), which is syntactically dependent on the aforementioned operator. After introducing the basic idea of the proposal, we apply it to standard SoT cases, as well as more complex cases of past temporal embeddings.

In Section 3, we provide a purely compositional implementation of our proposal in terms of presuppositional tense semantics.

Section 4 is devoted to demonstrating that the same mechanism can also be straightforwardly extended to present tense; An underspecified present tense proposal akin to the one proposed for past tense, i.e., containing an absolute and a relative meaning component, yields the correct semantics both for matrix and embedded tenses, including challenging embeddings.

Section 5 concludes.

2 Past tense proposal

2.1 Introducing the components

We start our analysis with the well-established observation that past tense takes higher scope than its surface position on the finite verb (Klein, 1994; Ogihara, 1996; Abusch, 1997; Kusumoto, 1999, 2005; von Stechow, 2002; Stowell, 1995, 1996, 2007; Zeijlstra, 2012). Evidence for such a scopal ordering of past tense comes, for instance, from examples like the following:

(9) Wolfgang played tennis on every Sunday. (von Stechow, 2006)

The intended interpretation of (9) is one where past tense outscopes the distributive quantifier *every Sunday*, which in turn outscopes the lexical verb *play*, yielding the paraphrase in (10a). The scopal order where past tense would take scope at its surface position, i.e., under *every Sunday*, amounts to the reading in (10b), which is absent (cf. von Stechow, 2002, 2005; Zeijlstra, 2012).

- (10) a. 'There exists a past interval t such that for every Sunday in t, Wolfgang plays tennis.'
 - b. *'For every Sunday, there exists a time before it such that Wolfgang plays tennis at that time.'

That there exists a covert past tense operator outscoping the distributive quantifier in (9) can furthermore be shown by expressing the operator explicitly. Crucially, the resulting sentence is truth-conditionally equivalent to (9):¹

(12) In the past, Wolfgang played tennis on every Sunday.

From the correct reading in (10a) it becomes evident that the distributive quantifier takes scope from an intermediate position between the lexical verb and the past operator, clearly revealing the dichotomy between the locus of semantic interpretation and the locus of morphological instantiation of past tense. Therefore, we assume—again in line with many others (e.g., Kusumoto (1999, 2005); von Stechow (2003); Stowell (1995, 1996, 2007); Zeijlstra (2012))—that the past tense morpheme does not carry canonical past tense semantics. Instead, we propose alongside them that 'real' past tense meaning, i.e., anteriority, is contributed by a structurally higher, covert past tense operator Op-PAST, whose presence is triggered when past tense morphology is used. One important role of past tense morphology is then to indicate the existence of a structurally high past tense operator. Syntactically, such a relation is commonly implemented by assuming past tense morphology

¹We thank Jacopo Romoli and Manfred Krifka (p.c.) for independently pointing out that there exist scenarios in which the fact that past tense usually takes highest scope does not always hold true. Consider the following utterance, addressing a person who keeps re-telling the same story, but reliably changes their role in it. In such a context, we understand the distributive quantifiers in (11) to raise across the past tense:

⁽¹¹⁾ Every Sunday you were a hero, but every Monday you were a coward.

to carry an uninterpretable feature, [uPAST], which is checked by a matching interpretable feature, [iPAST], carried by Op-PAST. We assume this covert past tense operator to carry the following semantic content:²

(13) $\llbracket Op\text{-}PAST \rrbracket = \lambda P. \ \lambda t^*. \ \exists t < t^* \& P(t)$

Op-PAST places the predicate P at a time t prior to some evaluation time t^* . At the matrix level, t^* by default applies to t_u and for the sake of simplicity we will take *Op-PAST* to denote [λP . $\exists t < t_u \& P(t)$] in these cases. Later in this paper we will discuss examples in which the value deviates from the default, though, providing evidence for the necessity of the more complex definition of *Op-PAST* given in (13).

We crucially depart from other approaches by building up on the fact that even though the locus of past tense is different from its overt instantiation—i.e., the tense marker -ed—, this does not entail that the past tense morpheme is semantically vacuous. There is nothing that *a priori* forbids the past tense morpheme to bring in an additional meaning component. Concretely, we take the meaning of a past tense morpheme, like -ed, to be comprised of two components: a syntactic feature [uPAST], which encodes a syntactic dependency with a higher past tense operator (as discussed above), and a semantic element that we assume to have the meaning of a relative non-future (cf. (14)). Both the covert operator and the past tense morpheme are thus semantically active (just as in syntactic dependencies like binding of an anaphor by an antecedent, or when movement leaves a trace, both participants in the dependency are semantically active (see also Kusumoto, 2005)).

Semantically, the past tense marker (-ed) for us then encodes a relative non-future meaning with respect to its closest c-commanding tense node (informally: 'not later than'), an assumption that will ultimately lead to the underspecified interpretation of past-under-past embeddings we propose. Formally, we assign the following denotation to the past tense marker:

(14) $\llbracket -\text{ed} \rrbracket = \lambda P. \ \lambda t. \ \exists t' \leq t \& P(t')$

In this context, the expression $t' \leq t$ is taken to mean that the lower boundary of the time interval t' is not later than the lower boundary of the time interval t. Hence, the run time of an event starting at time t' lies either strictly before or exactly at the starting of the run time of an event happening at time t.

With these assumptions in place, a mono-clausal past-tensed sentence such as *Susan loved her mother* receives the following interpretation (again presented somewhat informally; see Section 3 for a formal derivation):

(15) Susan loved her mother.

a. $[Op - PAST_{[iPAST]} [-ed_{[uPAST]} [Susan love her mother]]]$ $\exists t' < t_u \qquad \exists t^2 \le t'$ b. $\exists t' < t_u \& [\exists t^2 \le t' \& love(Susan, her mother, t^2)]$

 $^{^{2}}$ Here we only present the intuition in operational terms. A full compositional analysis of the facts, which will be cast in presuppositional terms, will be spelled out in Section 3.

c. There is a time t' strictly before the utterance time t_u and Susan's loving her mother starts at a time no later than t'.

Note that the proposed analysis makes no hard commitment with respect to whether Susan loves or fails to love her mother at/after t_u ; rather, it restricts the contexts in which (15) can be felicitously uttered to those in which Susan's loving her mother started prior to t_u . The proposal is therefore fully compatible with the well-established fact that even though a past-tensed stative sentence may trigger the inference that the described state has ceased to hold, it never entails that (see Altshuler, 2016, for discussion and overview).

Our proposal deviates from standard analyses in that it introduces vagueness with respect to the ordering of t' and t^2 in simple past-tensed sentences: They either refer to the same point in time or the latter precedes the former; In this sense, a clause containing a single past tense morpheme should be able to yield both a regular past tense interpretation and an interpretation very close to that of a past perfect (albeit in the case of a past perfect reading, the intermediate t' must be a *salient* reference time, whereas this is not required, though possible, for our simple past tense interpretations). At first sight, this seems like a counterintuitive complication of the meaning of past tense. However, this additional relative non-future semantics of the past tense morpheme may receive some actual empirical support. Let us reconsider sentence (15). The most prominent interpretation of the sentence, a simple past reading (*Susan loved her mother at a time prior to* t_u), is derived in case that t' and t^2 are taken to refer to the same point in time, constituting the default case. Crucially, though, there are contexts in which a speaker may choose to use a simple past-tensed sentence even though the interpretation she wants to trigger is actually more comparable to a past perfect one and, thus, t^2 is to be interpreted to precede t'. One such context is the following:

- (16) a. Did Susan go to today's 4pm class?
 - b. No, she left for Spain.

The intended interpretation of (16b) is one that places Susan's leaving for Spain *prior to* 4pm today. The intermediate time interval t' here may act as a reference time in the sense of Reichenbach (1947).

Most likely due to pragmatic blocking effects, this ambiguity of past tense usually remains unnoted in unembedded sentences as the same information can, more transparently, be expressed via a past-perfect construction. Hence, the question arises why single past tense readings should be able to give rise to such readings in the first place. It could in principle very well be the case that any reading where t^2 precedes rather than overlaps t' is pragmatically blocked. Interestingly, however, the preference to use past perfect over simple past tense in contexts like (16) seems to decline with time, as has been shown in literature on language change (cf., e.g., Bowie, Wallis, and Aarts (2013); Gorrell (1995); Michaelis (1998)). For instance, Bowie et al. (2013) reports a significant decline of the past perfect across contexts (-34% per-million-words frequency across two subcorpora³), mostly at the expense of present perfect and simple past tense forms. Closer analysis of the relevant contexts lets

³ Bowie et al. (2013) investigates the change in usage of the (general) perfect in spoken standard British English based on the *Diachronic Corpus of Present-day Spoken English (DCPSE)*, a spoken, mainly British, English corpus. The corpus is comprised of two subcorpora, the *London–Lund Corpus (LLC)* and the

them conclude that there seems to be an "increasing tendency to choose the past non-perfect [i.e., simple past] in main clauses, relative clauses, and temporal clauses [where, historically, past perfect was used]" (Bowie et al., 2013). The observation that the simple past tense can convey readings that in earlier days were arguably only expressed by past perfects is fully in line with our proposed past tense semantics. In (17) we present some examples from Bowie et al. (2013) where the more transparent past perfect tense traditionally would have been used but now is not.

- (17) a. They sent one to my mother after she *died* or something.
 - b. so I just took uh some of the tablets you gave me and it cleared up within two days
 [Context indicates the giving of the tablets preceded their taking by as much as a

[Context indicates the giving of the tablets preceded their taking by as much as a year.]

Contexts such as (16) as well as the examples cited from the literature on language change in (17) lend plausibility to a past tense semantics that explains both usual past tense readings and readings that are closer to a past perfect. Although further work should establish the exact semantic restrictions which enable/prevent the interchangeability between simple past and past perfect forms in a given context, we take this data as tentative support for an underspecification account of past tense.

2.2 Accounting for sequence of tense

In this section, we show that the proposed past-tense semantics renders a mechanism that explains the systematic ambiguity between the sim and the b-s readings of past-under-past embeddings without postulating past-tense meaning deletion. The crucial advantage of this approach over other syntactic-semantic approaches of SoT is then that it does away with the assumption that the two readings are truth-conditionally distinct, an assumption which has recently been called into question by, e.g., Altshuler and Schwarzschild (2012); Altshuler (2016). In contrast to most of the literature (modulo Altshuler and Schwarzschild (2012); Altshuler (2016)), the proposal introduced here thus retains a one-to-one mapping between past tense form and meaning, a feature which makes it desirable from a compositional semantic point of view.

As a starting point for the analysis of sentences that contain more that one instance of past tense morphology, we follow Zeijlstra (2012), who proposes that the number of covert operators is regulated by economy principles: We assume that a covert operator (here Op-PAST) may only be included when grammatically necessary. Since a single covert past tense operator can in principle check off all of the uninterpretable past tense features in its syntactic domain via multiple agree—like any other covert operator—, a sentence with a past tense morpheme in both the matrix and an embedded clause in principle requires the presence of only one past tense operator. In (18), Zeijlstra's economy constraint thus entails that one Op-PAST will check all present [uPAST] features and no further Op-PAST may be included.

British Component of the International Corpus of English (ICE-GB), collected several decades apart, i.e., 1950s–1970s and 1990s, respectively, which enables the study of language change across this time interval.

Only when two [uPAST] features appear in different syntactic domains is the inclusion of a second Op-PAST allowed, and even necessary, as we will see later on.

The fact that only one past operator is required for the analysis of past-under-past constructions, together with the relative non-future semantics we attribute to past tense morphology, explains why every past tense embedded under another past tense is compatible with both a sim and a b-s reading: Such a configuration yields a totally ordered set of tense nodes from the matrix past operator to the most embedded past tense:⁴

- (18) John said Mary was ill.
 - a. [$Op-PAST_{[iPAST]}$ [$-ed_{[uPAST]}$ [John say [$-ed_{[uPAST]}$ [Mary be ill.]]]]] $\exists t' < t_u \qquad \exists t^2 \le t' \qquad \exists t^3 \le t^2$
 - b. $\exists t' < t_u \& [\exists t^2 \le t' \& say(John, t^2, [\exists t^3 \le t^2 \& be-ill(Mary, t^3)])]$
 - c. John's saying is strictly before the utterance time t_u and Mary's being ill starts out no later than at the time of John's saying.

As was the case for mono-clausal sentences, the covert past tense operator in (18) places the sentence proposition at some time $t' < t_u$, providing the head of the tense chain. Both instances of past tense morphology semantically express a relative non-future with respect to their closest c-commanding tense node. The time t^2 is interpreted as a relative nonfuture with respect to t', and t^3 constitutes a relative non-future with respect to t^2 . The b-s reading of (18) then arises in case that $t^3 < t^2$, while the sim interpretation is yielded for $t^3 = t^2$. The systematic availability of both readings for past-under-past constructions receives a principled explanation in terms of semantic underspecification and not in terms of LF-ambiguity in this way. Note that it also immediately follows that the f-s reading in which t^3 would be temporally located between t^2 and t_u —cannot be derived since our approach only takes every past tense morpheme to refer to a time interval no later than the closest c-commanding evaluation time.

2.3 Evaluating the proposal

2.3.1 Future reference of past tense morphology in other configurations

The previous section has shown that our account yields the correct results for standard SoT sentences: It derives the sim and the b-s, but crucially not the f-s readings for past-under-past embeddings. We have also proven that the proposal still makes correct predictions for monoclausal past-tensed sentences. Nevertheless, it is received wisdom that any theory of SoT additionally has to account for more complex cases of temporal embeddings, e.g., special cases in which an embedded past tense morpheme does receive a future-oriented interpretation or an interpretation that seems to be temporally independent from the closest evaluation time. This subsection and the next are devoted to demonstrating how our approach deals with such challenging SoT sentences, starting with the behavior of past tense in complement clausal

⁴Note that for purposes of illustration we take *say* to be extensional here, though we are completely aware that it is actually an intensional predicate (see Section 3, as well as, e.g., Pearson (2015) and references therein). Nothing in our analysis hinges on that, though

embeddings, and moving on to the interpretation of past tense in (non-)restrictive relative clauses and certain cases involving ellipsis.

Future reference in past-under-past configurations involving woll

We begin with the well-established observation that—seemingly in contrast to what was said above—past-embedded past tense can in fact sometimes make reference to a time interval that strictly succeeds the matrix time in English. Examples of such future-reference past tense uses include the following:

- (19) John said he would buy a fish that *was* still alive. (Ogihara, 1989)
- (20) He decided a week ago that in ten days he would say to his mother that they *were* having their last meal together. (Abusch, 1988)

In their most prominent readings, the most embedded past tense forms, i.e., was and were, express simultaneity with respect to the time of buying and the time of saying, respectively. The challenge such examples pose to SoT accounts stems from the fact that these times have been shifted to a time later than the matrix time by means of would (cf., a.o., Abusch, 1988, 1997; Ogihara, 1989, 1995). As a result, was and were, even though carrying past tense morphology, receive a future-reference interpretation with respect to the matrix time.

Importantly, for temporal configurations as in (19) and (20) future-reference interpretations are possible, and the most prominent ones. Yet, in the absence of temporal modifying adverbs, such as *still* in (19), the order of events is first and foremost underspecified. For example, without the temporal modifier *still*, sentence (19) could be felicitously uttered in case the fish is alive at the time of buying, in case it was alive shortly before the buying event but after the saying event, or arguably even in case it was alive prior to the saying event. Our approach successfully captures the multiple interpretations of such 'fish-sentences' under the assumption that *would* is the conflation of *woll*—a tense operator that places the evaluation time of a proposition in the relative future of the sentence's current evaluation time (cf. Abusch, 1988; Ogihara, 1996; Condoravdi, 2002) (cf. 21)— and a [uPAST] feature, which restricts its occurrence to past tense sentences^{5,6}.

(21) $\llbracket \operatorname{woll} \rrbracket = \lambda P. \ \lambda t. \ \exists t'. \ t' > t \ \& \ P(t')$

Under these assumptions, (19) receives the following interpretation:

(22) John said he would buy a fish that was alive.

a. [
$$Op-PAST_{[iPAST]}$$
 [$-ed_{[uPAST]}$] John say [$woll_{[uPAST]}$] he buy a fish [that
 $\exists t' < t_u \qquad \exists t^2 \le t' \qquad \exists t^3 > t^2$
[$-ed_{[uPAST]}$ [be alive.]]]]]]]]
 $\exists t^4 \le t^3$

⁵Here, we ignore the modal contribution of the operator *woll* in terms of universal quantification over possible worlds (cf., e.g., Ippolito, 2013), which is orthogonal to the analysis presented in this paper.

⁶The reason why *would* is a conflation of *woll* and a [uPAST] feature and not of is the conflation of *would* and a past tense morpheme, is that *woll* by itself already makes a temporal contribution.

- b. $\exists x \ [\ \text{fish}(x) \& \exists t' < t_u. \exists t^2 \leq t' : \text{say}(\text{John}, t^2, [\ \exists t^3 > t^2 : \text{buy}(\text{he}, x, t^3) \& \exists t^4 \leq t^3: \text{ be-alive}(x, t^4)])]$
- c. There is a time t^4 which is the time of a contextually salient fish's being alive, and t^4 is prior or equal to some time t^3 . The time t^3 is the time of John's buying the fish which lies strictly after t^2 , i.e., the time of John's saying event. t^2 is prior or equal to t' which, in turn, is a time strictly before the utterance time t_u .

What is essential about this analysis is that the most embedded past, i.e., was, is ordered prior or simultaneous to the time of the buying, and not prior or simultaneous to any other time, such as the matrix time or the utterance time. This correctly allows for a laterthan-matrix interpretation of the embedded past tense, but does not necessarily entail a later-than-utterance time interpretation. The derived interpretation is, hence, compatible with all of the readings (19) may have. The same holds for example (20):

- (23) He decided (a week ago) that (in ten days) he would say to his mother that they were having their last meal together.
 - a. [$Op-PAST_{[iPAST]}$ [$-ed_{[uPAST]}$] [He decide [$woll_{[uPAST]}$] [he say to his mother [that $\exists t' < t_u \qquad \exists t^2 \le t' \qquad \exists t^3 > t^2$ [$-ed_{[uPAST]}$] [they be having their last meal together.]]]]]]]] $\exists t^4 \le t^3$
 - b. $\exists t' < t_u \& [\exists t^2 \leq t' \& \text{decide}(\text{he}, t^2, [\exists t^3 > t^2 \& \text{say-to-his-mother}(\text{he}, t^3, [\exists t^4 \leq t^3 \& \text{be-having}(\text{they, last meal together}, t^4)])])]$
 - c. There is a time t^4 which is the time of their last meal, and t^4 starts no later than some time t^3 . The time t^3 is the time of his saying and lies strictly after t^2 , i.e., the time of his deciding. t^2 is prior or equal to t' which, in turn, is a time strictly before the utterance time t_u .

Even when neglecting the temporal modifiers, which unambiguously place the time of the meal in the future, the formula derived from the tense nodes within the sentence already shows that the time of the meal is not restricted to a past interval. As it is ordered relative to the f-s time of the saying event, the time of the meal can lie strictly after t_u .⁷

Future reference in past-under-past configurations without woll

Another set of challenging data which evokes a future interpretation for a past-embedded past tense in a complement sentence consists of sentences like the following:

(24) He hoped she *tried* to kill him first.

(Klecha, 2016)

The novel challenge posed by these examples is that they have an interpretation akin to that of (19) and (20), even though they do not contain an overt future-shifter, like *woll*. Naturally,

⁷Note that for (20), the b-s relation between the most embedded past tense and its c-commanding tense node (i.e., the time of saying) appears to absent. This is however is due to additional aspectual information, namely imperfective aspect on *having*). Since disambiguation is achieved through aspect and not tense, such blocking does not provide a problem for the proposed analysis but rather shows how underspecification can be resolved in practice.

if you can still hope, you have not been killed yet, meaning that, temporally, the hoping event expressed in (24) takes place prior to the potential killing event. Klecha (2016) argues that the availability of such an independent future-shifted interpretation of the embedded past tense is restricted to predicates that already have an inherent modal future orientation built into their semantics, like *hope* or *pray*. By contrast, Klecha proposes that predicates like *think* impose an upper limit on the temporal possibilities of their prejacents and therefore the temporal possibilities of their complement clauses, as they cannot themselves introduce a similar future-shifted interpretation in the absence of another modal (cf. Abusch's *Upper Limit Constraint* (1997)).

Klecha's (2016) implementation of this insight relies on the observation that futureoriented attitudes like *hope* deviate from other, non-future-oriented attitudes like *think*, in the choice of modal base pronouns they may combine with. Modal bases determine the set of worlds which are accessible from a given point in time (Kratzer, 1981, 1991), and Klecha (2016) claims that only two different modal bases exist: a doxastic one, which imposes an upper limit on its prejacent's temporal orientation via quantifying over *actual* histories, and a circumstantial one, which does not impose such a limit and instead maps the prejacent's time and a history to the set of all possible *future* histories departing from that time. Crucially, Klecha argues that attitude verbs like *think* may only combine with a doxastic modal base, whereas *hope* and *pray* may also combine with a circumstantial modal base, explaining the possible f-s interpretations of their complement clauses.

Our proposal is in full accordance with Klecha's view. Although the past tense morphology on *hope* in (24) places the time of the matrix sentence prior to the utterance time, as a future-oriented predicate *hope*, by itself, can shift the evaluation time of its complement proposition to a future point in time—even in the absence of *woll*.

(25) He hoped she tried to kill him first.

a.
$$\begin{bmatrix} Op-PAST_{[iPAST]} & [-ed_{[uPAST]} & [He hope & [-ed_{[uPAST]} & [she try to kill him \\ \exists t' < t_u & \exists t^2 \le t' & \exists t^3 \ge t^2 & \exists t^4 \le t^3 \\ first & []]] \end{bmatrix}$$

In our proposal, this inherent future-orientation of *hope* and *pray* is hard-wired into their semantics. Note that we are not dependent on this implementation of Klecha's proposal; Any type of inherent future semantics as part of the lexical meaning of such predicates, be it via modal bases or otherwise, can derive these facts under our analysis.

As a result of the inherent future shift, our analysis derives the correct meaning of such future-shifted sentences similar as in (19) and (20): Since the forward-shifted evaluation time t^3 is introduced in the matrix clause (which can lie strictly after the time of utterance t_u), the verb *tried* then simply means *tried at time* t^4 , whereby t^4 is no later than t^3 and can also lie in the strict future of t_u . One caveat of the implementation we choose is that we also predict an unattested reading of (24) to be available, i.e., one in which the killing takes place prior to the hoping (e.g., in the case that $t^4 < t^3 = t^2 = t' < t_u$). Whereas the availability of such a temporal ordering is crucial for us in order to derive the correct semantics for sentences like (26), which Klecha (2016) would solve via a different modal base, for the case under discussion we rely on pragmatics, e.g., the addressee's knowledge that hoping requires not having been killed yet, to independently block such readings.⁸

(26) John hoped (at 4pm) she got there on time (at 3pm).

Future reference in past-under-future configurations

The last instance of embedded past tense morphology receiving a future interpretation we discuss concerns cases where past tense is embedded under a future matrix predicate (cf. (27)). Such past-under-future constructions again give rise to different readings: In some, the past tense is assigned its canonical 'prior to time of utterance'-interpretation (cf. (27a)). Crucially, however, in the most prominent reading of (27), the past-marked predicate takes place after the utterance time (cf. (27b))—a reading which poses a challenge to most SoT theories.

- (27) Alan will think everyone hid.
 - a. (Tomorrow) Alan will think everyone hid (yesterday).
 - b. (Tomorrow at 3pm) Alan will think everyone hid (tomorrow at 2pm).

An important observation that can be made with respect to the analysis of such sentences is that the tense shifter *woll* is instantiated as *will* in this context. As a result, it becomes evident that Op-PAST cannot take higher scope than the *woll*, as otherwise it would be spelled out as *would*. This immediately entails that *will* cannot carry a [uPAST] feature. As part of his economy principle, Zeijlstra (2012) proposes that an operator needs to be included in the closest possible position above the highest instance of the uninterpretable feature it checks. Since *will* does not carry a [uPAST] feature that Op-PAST could check (but rather a feature [uPRES], see Section 4), the operator is included above the highest instance of [uPAST], i.e., in the complement clause. As a result, the underlying syntactic structure of (27), for now, must be the following (cf. also Heim, 1994):

(28) [Alan will think [$Op-PAST_{[iPAST]}$ [$-ed_{[uPAST]}$ [everyone hide]]]]

Uncontroversially, we take the semantics of *will* to be the same as those for *would* (cf. (21)), modulo the [uPAST] feature, which restricts it to past environments. Hence, *will* shifts the evaluation time of its prejacent to a point in time which succeeds the evaluation time it receives as its input. Sentence (27) does not specify an evaluation time for *woll*'s relative argument t, e.g., by means of a modifying clause or an embedding predicate; The variable thus gets valued against its default value t_u . Under these assumptions, the correct interpretation of (27) is yielded in the following way:

(29) Alan will think everyone hid.

⁸Note that past tense futurates embedded under a higher past do not count as making a future reference under past tense. A sentence like *Mary said the Red Sox were playing the Yankees tomorrow* means that already at the time of saying there is a state where it is intended that the Red Sox are playing the Yankees tomorrow. Futurates always refer to events that are already planned or settled to take place at the time denoted by grammatical tense, see Copley (2008, 2018); Kaufmann (2015)

- a. [Alan will think [$Op-PAST_{[iPAST]}$ [$-ed_{[uPAST]}$ [everyone hide]]]] $<math>\exists t' > t_u \qquad \exists t^2 < t' \qquad \exists t^3 \le t^2$
- b. $\exists t' > t_u$ & think(Alan, t', [$\exists t^2 < t'$ & $\exists t^3 \le t^2$ & hide(everyone, t^3)])
- c. There is a time t' in the strict future of t_u and Alan thinks at t' that there is a time t^2 earlier than t' such that everyone from a contextually salient group hid at a point t^3 no later than t^2 .

The evaluation-time shifter *will* takes scope over the past tense operator and changes the evaluation time t^* of *Op-PAST* to a time in the future. It is from this future-shifted point in time that the past marker *-ed* introduces a no-later-than relation between the hiding event and the thinking event; no direct connection between the event time of the past-tensed predicate and t_u is thus established, which is why the hiding can lie in the strict future of t_u .

Note that if the operator Op-PAST entailed an absolute past ordering of the tense morphemes that it takes scope over with respect to the utterance time (i.e., if its denotation were $[\![Op-PAST]\!] = \lambda P$. $\exists t < \underline{t_u} \& P(t)$), sentences such as (27) could not be accounted for by our proposal. However, as seen in (13), the relation 'prior to time of utterance' is not cooked into the semantics of Op-PAST; Instead, the operator is defined as a relative past with respect to a time variable t^* , whose value may be t_u , but which can also refer to a time interval later than t_u , if introduced by an independent source.

2.3.2 Relative clauses

A further set of data for which embedded past tense morphology may evoke readings that are not anchored with respect to the evaluation time involves relative clauses. In certain relative clauses, as in example (30), the embedded past can yield any of the following readings: a b-s, a sim and a f-s one. Both past tenses independently refer to a time interval prior to the time of utterance.

(30) Mary met a woman who was president.

a.	In 2000, Mary	met a woman	who was	president in	1995.	[b-s	;]
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- b. In 2000, Mary met a woman who was president in 2000. [sim]
- c. In 2000, Mary met a woman who was president in 2004. [f-s]

Whereas Eng (1987) observed that relative clause tenses differ from complement clause tenses in allowing an independent, or absolute interpretation, Abusch (1988) showed that this only applies to relative clauses in extensional contexts. In intensional contexts, relative clauses can only trigger a f-s reading if they receive a *de re* interpretation (see also Ogihara, 1989, 1996). Under a *de dicto* construal, relative clauses behave similarly to complements of intensional contexts in only allowing a b-s or sim reading. As the reader can check, in (31a-b), both a *de re* and a *de dicto* reading are available, but in (31c), only a *de re* reading is yielded (see also Heim (1994); Ogihara (1995); Stowell (2007)):

- (31) Mary thought that she met a woman who *was* president. [b-s]
 - a. De re / de dicto: In 2000, Mary thought that she met a woman who was president in 1995. [sim]

- b. De re / de dicto: In 2000, Mary thought that she met a woman who was president in 2000.
- c. De re / *de dicto: In 2000, Mary thought that she met a woman who was president in 2004. [f-s]

To account for the differences in (31), we follow Stowell (2007) who argues that the de dicto/de re distinction is structurally encoded in terms of the LF position of the relative clause: outside or inside the CP complement of the intensional verb. Concretely, we entertain the hypothesis (in line with Stowell (2007), though also substantially different from it) that the past tense morpheme inside a relative clause that yields a *de dicto* reading can have its [uPAST] feature checked against a higher covert tense operator carrying [iPAST] inside the matrix clause, but that the past tense morpheme inside a relative clause that yields a *de re* interpretation cannot do so. Consequently, the latter requires a covert past tense operator of its own, with t^* being valued for the time of utterance. Therefore, a relative clause with a *de dicto* interpretation allows only a sim and a b-s reading (when containing past tense morphology embedded by a higher past tense clause), whereas a relative clause with a *de re* interpretation in the same situation yields sim, b-s, and f-s readings. This explains why the two past tense markers in (31) under a *de re* construal need to be evaluated independently of each other with respect to the time of utterance: The [uPAST] feature on the past tense morpheme inside the relative clause cannot be checked by the covert past tense operator that the matrix past tense morpheme agrees with, given that the relative clause is not in the c-command domain of the intensional predicate. Consequently, a second O_{P-PAST} must be included inside the relative clause. As this second operator in (31) cannot be bound by any higher tense operator, both past tense operators must refer to the time of utterance (Zeijlstra, 2012).

(32) Mary thought that she met woman who was president.

a. de dicto $[Op-PAST_{iPAST}] -ed_{uPAST}$ Mary think that $-ed_{uPAST}$ she meet a woman $\exists t' < t_u \qquad \qquad \exists t^2 \le t'$ $\exists t^3 < t^2$ who -ed_[uPAST] be president]] $\exists t^4 < t^3$ b. de re $[Op-PAST_{iPAST}] -ed_{uPAST}$ Mary think that $-ed_{uPAST}$ she meet a woman] $\exists t' < t_u$ $\exists t^2 < t'$ $\exists t^3 < t^2$ Op-PAST_[iPAST] -ed_[uPAST] be president] [who $\exists t^5 < t''$ $\exists t'' < t_u$

Naturally, the question arises whether this structural ambiguity should be restricted to relative clauses inside intensional predicates. If relative clauses can (covertly) raise to higher position and if the *de re* vs. *de dicto* interpretation of a relative clause in intensional contexts is the result of whether it raises or not, such raising should also apply in examples like (30). This seems indeed to be the case; even though there is no *de re* vs. *de dicto* distinction in the first place, the relative clause can be freely interpreted with respect to the time

of utterance. However, it is also predicted that (30) should be fine with the relative clause being able to have its internal [uPAST] feature being checked by the matrix operator carrying [iPAST]. This predicted ambiguity cannot be tested for examples like (30), as the b-s and sim readings are already available anyways. However, as we saw before, under past-underfuture constructions, past tense is able to take local scope and does not necessarily require an interpretation where it refers to a time that is prior to the time of utterance. This is also the case for relative clauses in past-under-future configurations. In (33), taken from Stowell (2007), the time of applying does not have to lie before the time of utterance under the *de dicto* reading.

(33) Sam will offer a job to a/any candidate [who filled out an application the day before].

Hence, (30) must have two logical forms: one with a raised relative clause that is outside the agree domain of matrix tense *Op-PAST*, and one where the relative clause is present within the agree domain of matrix tense *Op-PAST*. Both (simplified) LFs for (30) are provided below:

- (34) Mary met a woman who was president.
 - a. [$Op PAST_{[iPAST]}$ -ed_[uPAST] Mary meet a woman] [who $Op PAST_{[iPAST]}$ $\exists t' < t_u$ $\exists t^2 \le t'$ $\exists t'' < t_u$ -ed_[uPAST] be president] $\exists t^3 \le t''$
 - b. $\exists x \; [\operatorname{woman}(x) \& \exists t' < t_u. \exists t^2 \leq t' \; [\operatorname{meet}(\operatorname{Mary}, x, t^2) \& \exists t'' < t_u. \exists t^3 \leq t'' \; [\operatorname{president}(x, t^3)]]]$
 - c. There is a woman x and at t^2 , prior or equal to t' which, in turn, is a time strictly before the utterance time t_u , Mary met x, and at t^3 , prior or equal to t" which, in turn, is a time strictly before the utterance time t_u , x is president.
- (35) Mary met a woman who was president.
 - a. [$Op-PAST_{[iPAST]}$ -ed_[uPAST] Mary meet a woman [who -ed_[uPAST] $\exists t' < t_u$ $\exists t^2 \le t'$ $\exists t^3 \le t^2$ be president]]
 - b. $\exists t' < t_u$. $\exists t^2 \le t'$ [meet(Mary, t^2 , [$\exists t^3 \le t^2$. $\exists x$ [woman(x) & be-president(x, t^3)]])]
 - c. At t^2 , prior or equal to t' which, in turn, is a time strictly before the utterance time t_u , Mary is meeting a woman x, and at t^3 , prior or equal to t^2 , x is president.

Thus, under the assumption that the position in which a relative clause needs to appear to receive a *de re* interpretation is a position from which its internal [uPAST] cannot be checked by [iPAST] on matrix Op-PAST, it follows directly that relative clauses with a *de re* construal in intensional contexts and all relative clauses in extensional contexts behave temporally independent from their matrix clauses.

2.4 Comparison with other sequence of tense approaches

So far in this section we have introduced an alternative account of SoT that relies on underspecified tense semantics instead of ambiguity at the level of LF, and we showed that it fares at least equally well with respect to the different challenges English poses to SoT accounts as existing proposals. Nevertheless, the fact that our account can explain the data does not in itself justify its correctness. Given the impressive canon of SoT literature, an important question to answer is how the proposal compares to existing ones and whether it provides new insights or even advantages.

2.4.1 Comparing underspecification- and ambiguity approaches

When comparing our analysis to existing ambiguity SoT approaches, an immediate advantage that emerges on the theoretical side is that we do not have to postulate a difference between a real past and a surface past, which is, underlyingly, a present tense in disguise (cf., e.g., Abusch, 1988; Ogihara, 1989), a zero tense (cf. Kratzer, 1998), or something yet different. In order to account for the simultaneous reading of past-embedded past tense, most ambiguity analyses are forced to allow present tense morphemes to receive the morphological shape of a past tense morpheme under certain conditions, an assumption which is primarily stipulated (c.f., e.g. Abusch, 1988; Ogihara, 1989; Kusumoto, 1999; Stowell, 2007, and references therein), except for by Kratzer (1998), who embeds the assumption into the bigger picture of binding theory, where anaphors denote bound variables that inherit features of their antecedents at PF.

Via taking past tense morphology to be a relative non-future, the approach proposed in this paper can account for the same cases as the ambiguity proposals while retaining a clear one-to-one mapping between temporal form and temporal meaning. Further conceptual challenges for ambiguity proposals arise in light of questions such as why only past tense exhibits the proposed kind of ambiguity—and not present tense, too—, and why this putative homophony is a systematic, cross-linguistic phenomenon (see Stowell (2007) for further discussion).

In addition, empirically, advantages of our proposal reveal themselves in ellipsis configurations such as (36a), which are known to tease apart ambiguity and underspecification readings, or in conclusion sentences with coordinated subjects as given in (36b).

- (36) SCENARIO. At breakfast (earlier this morning), John said "Mary was ill a month ago," and Bill said "Mary is ill now."
 - a. During breakfast, John said that Mary was ill and Bill did so, too.
 - b. Therefore, during breakfast, both John and Bill said that Mary was ill (at some point).

Given the assumption of structural parallelism in ellipsis contexts, ambiguity approaches predict that (36a) may only be used in scenarios in which John and Bill both uttered the sentence *Mary is ill* or both uttered the sentence *Mary was ill*. This is because the LF of the elided clause must be identical to the LF in the antecedent. Since sim and b-s readings have different LFs in these approaches, the two readings should be the same for both clauses; They should both either yield a sim reading or a b-s reading. As a result, ambiguity approaches predict sentence (36a) to be unacceptable in the given scenario. Similarly, ambiguity approaches rule out the coordinated subject construction in (36b) as an adequate conclusion sentence in the provided context, since there exists a mismatch between the simultaneous report context set up by John's utterance and the backward-shifted one set up by Bill's utterance. Our proposal, on the other hand, rules it in as an adequate conclusion. We predict temporally mixed readings to be available for both (36a) and (36b) (of course, in addition to the temporally parallel ones). Hence, under the approach proposed in this paper, (36a) and (36b) must be acceptable.

Indeed, it appears that mixed readings such as in (36a) are available. Most of our informants accept sentences with coordinated subjects in scenarios such as (36b), even though native English speakers prefer (36) less without the modifier *at some point*. Crucially, all informants across the board have so far accepted the sentence with *at some point* in it. It is not straightforwardly clear how ambiguity approaches would explain this data (for a similar conclusion, see Sharvit (2018); though see also Bar-Lev (2014)).

The empirical predictions that the underspecification approach makes appear to be correct indeed. Given the theoretical and empirical advantages underspecification analyses exhibit over ambiguity approaches, we reject the hypothesis that SoT should best be explained in terms of LF ambiguity. Note that we are not the first ones to take a stand against this well-established ambiguity assumption, though. Altshuler's (2016) and Altshuler and Schwarzschild's (2012) pragmatic SoT proposal also assigns only one LF to both readings. As a next step, we shall, therefore, evaluate our analysis against theirs.

2.4.2 Comparison with existing non-ambiguity approaches

Like us, Altshuler (2016) and Altshuler and Schwarzschild (2012) assume that past-underpast embeddings of stative predicates are not ambiguous between a sim and a b-s reading. Unlike us, however, they propose that such configurations always, unambiguously, receive a b-s interpretation and that a true sim reading of past-embedded past tense does not exist. In fact, what is commonly referred to as the simultaneous reading of embedded past tense in the SoT literature for them only constitutes a canonical past reading that does not stand in competition with the present-tensed alternative of the same clause. Thanks to the lack of competition, they argue, such instances of past-tensed statives do not evoke their usual cessation implicature that the described state no longer holds, and therefore the perception of simultaneity arises.

To make the theory's core assumption more explicit, consider the following example.

(37) My heart was racing.

Even though nothing in the semantics of the sentence excludes the possibility that the author's heart is still racing at the time of utterance (under an existential theory of tense, the truth conditions of (37) are met as long as there exists some moment prior to t_u at which the author's heart was racing), we nevertheless understand that the described state no longer holds. According to Altshuler's (2016) and Altshuler and Schwarzschild's (2012) scalar theory of tense, this is the case since the utterance stands in Gricean competition with its present-tensed alternative My heart is racing (Grice, 1975).

Given such assumptions, now the question that arises for the scalar tense theory is why past tense morphology does not evoke cessation implicatures uniformly. For example, they have to explain why no cessation implicature is commonly calculated in the following sentence.

(38) The doctor said my heart was racing.

As before, the answer lies in the clause's competition with its present-tensed alternative, i.e., *The doctor said my heart is racing*. As it turns out, this alternative cannot function as a competitor for (38), given the fact that it yields a d-a reading, and it is exactly in those cases in which it cannot do so that Gricean reasoning does not advance to the stage at which a cessation implicature is drawn and the sentence, even though backward-shifted in semantic terms, is perceived to convey simultaneity.

A crucial assumption for (Altshuler, 2016; Altshuler & Schwarzschild, 2012) is that whenever a state holds at a point in time, it must necessarily also hold at another point in time, no matter how tiny, preceding it, something they refer to as The temporal profile of statives and stative-like predicates (TPS). Thus, whenever a state holds at the time of utterance, it must also have held at a moment prior to it, meaning that a present-tensed stative always asymmetrically entails its past-tensed counterpart. Even though our proposal makes similar predictions as Altshuler (2016) and Altshuler and Schwarzschild's (2012) with respect to the non-ambiguity of different past-under-past readings, it is also substantially different. For the scalar theory, for example, the TPS is a necessary assumption for the computation of a cessation implicature, as it places the present- and past-tensed version of stative clauses on a scale. At the same time, the TPS is not uncontroversial. It has been (implicitly) rejected in various existing semantic discussions of tense (cf., e.g., the discussion of lifetime effects in Musan (1997); Magri (2009, 2011); Thomas (2012) or the *earliest*-operator in Beaver and Condoravdi (2003)). Relatedly, the causal relation between the absence of cessation and a sim reading has recently been called into question by Sharvit (2018) based on data from Hebrew and Greek, where particular expressions can be conveyed both via an embedded present and via an embedded past tense, i.e., cases where the cessation implicature is predicted to emerge but does not do so. By contrast, our approach does not raise these concerns.

Nevertheless, even if we were to accept the TPS hypothesis, Altshuler (2016) and Altshuler and Schwarzschild's (2012) proposal would make different predictions from ours. Their proposal predicts that past-under-past embedded eventive predicates are always interpreted in a b-s and not a sim manner (as the TPS does not hold for eventives). Our proposal, by contrast, should allow for sim and b-s readings for both embedded eventive and embedded stative predicates—similar to many versions of the classical ambiguity theory, which also do not have stativity as a prerequisite for sim readings. A possible point of evaluation between the two non-ambiguity proposals is therefore provided by the presence or absence of simultaneous readings of past-embedded eventive predicates. We believe that our proposal is indeed on the right track as the claim that no embedded past eventive may receive a sim interpretation appears to be too strong for English.

That only stative predicates may receive a sim interpretation has, for example, been refuted by Kusumoto (1999). She argues, with Partee (p.c. to Kusumoto, as cited in Khomitsevich (2007)), that examples such as (39) have a sim reading even though they embed a past eventive verb:

(39) Elliott observed/noticed/perceived that Josephine got hurt.

(Kusumoto, 1999)

Simultaneous readings generally appear to be possible for verbs of perception (observe/notice/ *perceive*), even though for some speakers a b-s reading is still preferred.⁹ We take this to be due to the fact that in English, where there exists a grammaticalized imperfective-perfective distinction, the usage of perfective aspect in past-under-past constructions yields a preference for a b-s reading. This is because the imperfective grammatical competitor (i.e., *Elliott* observed that Josephine was getting hurt) or infinitival competitor (i.e., Elliott observed Josephine getting hurt) unambiguously triggers a sim reading due to its stativity property, and thus provides a more transparent way to express the desired reading. The fact that there exist such (aspectual) competitors in English, however, suggests that the absence of the sim reading in English past-under-past perfectives must be due to pragmatic blocking effects rather than being a property of past itself. The question then is why the sim reading under perception verb is less sensitive to these pragmatic effects than other verbs. We presume that this has to do with the lexical semantics of perception verbs (in general, you perceive something at the time it is happening). However, irrespective of the question of why certain verbs appear to be more sensitive to these blocking effects than under other verbs, the crucial thing is that since simultaneous readings are possible for eventive predicates, tense semantics must in principle allow for them and not forbid them (as is the case in Altshuler (2016)'s and Altshuler and Schwarzschild's (2012) system).

All in all, this section has shown that the SoT approach proposed here not only explains the relevant data points of embedded tense in English but also has clear advantages over alternative existing SoT analyses.

3 Formal implementation

After having introduced the proposal in slightly informal terms in the previous subsections, we now lay out a compositional, type-driven implementation of our account. For this, we follow Partee (1973) among many others in assuming that tense should be cast in presuppositional rather than a quantificational terms. Given their explanatory power regarding matrix tense phenomena as well as their intuitive appeal, pronominal analyses of tense morphology are well-established in the literature (Partee, 1973; Heim, 1994; Kratzer, 1998; Schlenker, 2003). Nevertheless, the behavior of embedded tense, i.e., the two-way meaning distinctions for both embedded present tense and embedded past tense, have always posed a notorious problem for such approaches. The reason for this is that traditionally these two-way meaning distinctions were taken to reflect LF-ambiguities, which would essentially block the way for embedded tenses to be interpreted straightforwardly in pronominal terms (cf. Abusch, 1997; Heim, 1994; Kratzer, 1998; von Stechow, 2009; Ogihara & Sharvit, 2012; Bar-Lev, 2014). However, since our analysis does not resort to LF ambiguity, nothing for us stands in the

⁹It was pointed out to us that predicates of communication may also have this effect: *The announcer* said that John struck out means 'The announcer said: "John strikes out".

way of a presuppositional analysis of embedded tense.¹⁰

(40)

We take Op-PAST to be the spell-out of a complex covert structure involving an anterioritypresupposition contributing temporal identity function (*Past*), a tense pronoun (1) and a context time-shifter (*T-shift*):



As stated before, we assume Op-PAST to carry the syntactic feature [iPAST], by means of which it syntactically licenses the presence of one or more past tense morphemes, -ed carrying [uPAST]—, in its syntactic domain. With our semantic implementation of Op-PAST we follow much of the established pronominal tense literature in assuming that tenses are the temporal analogue of pronouns, referring to times, whose reference is presuppositionally constrained (cf., e.g., Heim, 1994; Kratzer, 1998; Sauerland, 2002). Since in our proposal temporal features live purely in the syntax, constraining a past pronoun's reference to past times is presuppositionally realized by Past, a partial identity function on the domain of times which combines with a tense pronoun 1 and returns its input time solely in case that it lies strictly prior to the contextually given evaluation time t. Cooked into the denotation of Op-PAST is thus the commonly assumed, presuppositionally restricted tense pronoun in (41c):

(41) a.
$$\llbracket \operatorname{Past} \rrbracket^{g,t} = \lambda t' : t' < t. t'$$

b. $\llbracket 1 \rrbracket^{g,t} = g(1)$
c. $\llbracket \operatorname{Past}_1 \rrbracket^{g,t} = g(1)$, defined if and only if $g(1) < t$

Nevertheless, a past-restricted pronoun semantics is not the only meaning contribution of Op-PAST in our proposal. It furthermore enables the referentially-restricted pronoun it invokes to become the evaluation time of its complement clause. Since we assume that the evaluation time is part of the context, we therefore suggest that Op-PAST contains an additional component, i.e., an evaluation time shifter T-Shift. T-Shift takes scope over g(1)and, in case no presupposition failure arises and g(1) meets the anteriority presupposition, it relativizes the complement of Op-PAST to g(1) as its new evaluation time.

(42)
$$\llbracket \operatorname{T-shift} \rrbracket^{g,t} = \lambda t'. \ \lambda P. \ \llbracket P \rrbracket^{g,t}$$

All things considered, *Op-PAST* then receives the following presuppositional denotation:

(43)
$$\llbracket Op\text{-}PAST \rrbracket^{g,t} = \lambda P : g(1) < t. \llbracket P \rrbracket^{g,g(1)}$$

¹⁰This does not mean that we exclude the possibility that our analysis cannot be cast in quantificational terms. Given the fact that a quantificational analysis can be amended with contextual restrictions on the domain of times the tense quantifies over (Stalnaker, ctd. in von Fintel & Heim, 2011) or default existential operators that bind pronominal tenses, the data can in principle be analysed in terms of both a presuppositional and an operational view of tense semantics.

Similar to our treatment of Op-PAST, we take the past tense morpheme -ed to be the spell-out of a complex lower head: It is also mother to a partial temporal identity function and a tense pronoun. In contrast to Op-PAST's partial identity function, Past, however, the temporal identity function, RNF, which -ed invokes, contributes a relative non-future presupposition to the semantics (cf. (45a)).

(44)
$$-ed_i$$

$$RNF_{\langle i,i\rangle} 2_i$$

Jointly, the terminal nodes of the treelet -ed make up the past tense morpheme's semantics as in (45c):

(45) a.
$$\llbracket \operatorname{RNF} \rrbracket^{g,t} = \lambda t' : t' \leq t. t'$$

b. $\llbracket 2 \rrbracket^{g,t} = g(2)$
c. $\llbracket -ed \rrbracket^{g,t} = g(2)$, defined iff $g(2) \leq t$

In a nutshell, we thus propose that Op-PAST takes a proposition of type $\langle s, t \rangle$ as its input and shifts its evaluation time t to a pronoun g(1) that is presupposed to be earlier than t, and each past tense morpheme -ed is a pronoun of type i that comes with a presupposition that it is no earlier than the t.

Under such assumptions, a simple past-tensed sentence like *Mary was ill* receives the logical form as in (46) and, as a result, the meaning in (47).

(46)



(47) $[[(46)]]^{g,t} = \lambda w : g(2) \le g(1) \land g(1) < t.$ be-ill(Mary, g(2), w)

The semantics in (47) say that Mary is ill at a time interval g(2) that is presupposed to be earlier than the local context time t. This is indeed the meaning that pronominal approaches to tense assign to such a sentence, as well.

Assuming say to have the (simplified) denotation in (48), the semantics spelled out in (41)-(45), yield the LF in (49) and the respective denotation in (50) for an SoT sentence like John said Mary was ill.

(48)
$$[\![\operatorname{say}]\!]^{g,t} = \lambda P. \ \lambda x. \ \lambda t'. \ x \ \operatorname{says} [\![P]\!]^{g,t'} \ \operatorname{at} t'$$



(50) $[[(49)]]^{g,t} = \lambda w : g(3) \le g(2) \land g(2) \le g(1) \land g(1) < t.$ say(John, be-ill(Mary, at g(3) in w), at g(2) in w) 'John said prior to t_u that Mary's illness started no later than his saying time.'

Even though our proposal, including *T*-shift, is fully presuppositional, we would like to point out that it could also be implemented without any operational component: Such an alternative implementation of the same idea in pronominal terms may, for example, involve making use of doubly-indexed pronouns (cf. Ogihara & Sharvit, 2012; Sharvit, 2018; Bar-Lev, 2014). According to this tradition, each tense is a pronominal expression that requires two times for its interpretation and, as a consequence, carries two indices. Crucially, the first index, denoting the event time, can be free, whereas the second, denoting the evaluation time, must be λ -bound. Under such assumptions, the following denotations for *Op-PAST* and *-ed* can be provided:

- (51) $\llbracket Op\text{-}PAST_{i,j} \rrbracket^g = g(i)$, defined if and only if g(i) < g(j)
- (52) $[\![-ed_{k,l}]\!]^g = g(k)$, defined if and only if $g(k) \le g(l)$

Self-evidently, Op-PAST under such an approach no longer contains an operational component. At the same time, it can be easily verified that this implementation also generates equivalent readings to the one introduced above. Since the two implementations make equivalent predictions, we will keep with the *T*-Shift version for the rest of this section, mostly for ease of presentation.

Either way, the proposal thus predicts the meaning of the sentence John said Mary was ill to be defined only if the time of John's saying event is no later than some time interval in the past and Mary's illness takes place no later than John's saying. It thus correctly explains that the sentence is true in both a simultaneous and a backward-shifted context. As we have shown before, with these proposed meanings for Op-PAST and past tense morphology, all other relevant examples involving past-under-past embeddings follow as well,

4 Extending the proposal to present tense

4.1 Introducing the components

As has been stated in the introduction, even though the alleged ambiguity of embedded past tense morphology has received a lot of attention in the literature, the present tense morphology puzzle seems to have been discussed less extensively so far. Nevertheless, we argue in this section that they can be analyzed on a par. Such a unified treatment of pastand present tense morphology will be able to capture both of the tenses' undergeneralized meaning and thus incorporate an absolute as well as a relative meaning component. The proposal laid out in the previous section, which disentangles the different meaning components of the past tense via outsourcing its 'real' past meaning, i.e., anteriority, into a high, covert past operator (*Op-PAST*) while encoding its relative past meaning, i.e., non-future, into the actual past tense morpheme (-*ed*), is compatible with this objective. In this section, we show that a similar mechanism can also account for the behavior of embedded present tense.

We start our discussion of present tense morphology with a reminder of the conundrum it poses across different embedding contexts. For this, reconsider the sentences in (8), repeated for convenience in (53):

The crucial observation is that the present tense morphology on *is* has a different semantic effect in the two sentences: In (53a) it evokes a simultaneous (sim) reading, meaning that it expresses simultaneity solely with respect to its evaluation time, i.e., the time of John's saying. Sentence (53a) can thus be felicitously paraphrased as follows: John, at some t later than t_u : "Mary is ill (now)." In (53b), by contrast, the present tense receives a double-access (d-a) reading: It is understood to express simultaneity with respect to both the utterance time and the evaluation time, i.e., the time of John's saying. As a result, (53b) is true if the state of Mary's being ill stretches from the time of John's saying event at some t prior t t_u to at least t_u itself. These embedding environments reveal that, just like past tense morphology, present tense morphology must also be underspecified in meaning.

In order to explain the observed behavior of present tense morphology, we propose a strategy along the lines of our proposal for past tense. In the following, we again first lay out more informally the intuition in quantificational terms before providing a presuppositional, compositional analysis. We assume that present tense, too, consists of two ingredients: a covert present tense operator and a semantically active present tense morpheme that agrees with this operator. It was shown in Section 2 that past tense takes scope outside vP, evidencing that (past) tense is not interpreted in the base position of the past tense morpheme. As a result we assume also for present tense that, syntactically, each present tense morpheme carries an uninterpretable present feature [uPRES] to be checked by a covert present tense operator (*Op-PRES*) carrying the interpretable feature [iPRES]. Semantically, we make the following assumptions for the two ingredients. First, similar to our proposal for

past tense morphology, each instance of present tense morphology (denoted for convenience by -s in the following) encodes simultaneity with respect to its respective evaluation time and thus functions as a relative meaning component of present tense. Simultaneity is hereby encoded in terms of time interval inclusion (where $t' \supseteq t$ means that the time interval t is included in or equal to t'):

(54) $\llbracket -s \rrbracket = \lambda P. \ \lambda t. \ \exists t'. \ t' \supseteq t \ \& \ P(t')$

Second, different from our account of past tense, but following ideas from Heim (1994) and Altshuler (2016), we propose that the high, covert present tense operator (*Op-PRES*), which encodes the 'real' present tense meaning, fulfills a *dual* role: It establishes an inclusion relation with respect to both its evaluation time, t^* , and the utterance time t_u . Accordingly, we take its denotation to be as follows:

(55)
$$\llbracket Op\text{-}PRES \rrbracket = \lambda P. \ \lambda t^*. \ \exists t'. \ [t' \supseteq t^* \& t' \supseteq t_u] \& P(t')$$

As was the case with past tense, at matrix level t^* applies to t_u by default. If this applies (as, e.g., in (57) and (59)), then the two tense restrictions *Op-PRES* introduces coincide and simplify to a purely absolute semantics of the operator:

(56)
$$\begin{bmatrix} Op-PRES \end{bmatrix}(t_u) = \lambda P. \exists t'. [\underline{t' \supseteq t_u \& t' \supseteq t_u}] \& P(t') \\ = \lambda P. \exists t'. t' \supseteq t_u \& P(t') \end{bmatrix}$$

Based on these assumptions, we predict a simple present-tensed sentence like (57), which places an event unambiguously at the utterance time, to have the following interpretation:

- (57) John is running.
 - a. $[Op-PRES_{[iPRES]}$ $[-s_{[uPRES]}]$ [John be running]]] $\exists t'. [t' \supseteq t_u \& t' \supseteq t_u] \quad \exists t^2 \supseteq t'$
 - b. $\exists t' \supseteq t_u \& [\exists t^2 \supseteq t' \& \text{be-running(John, } t^2)]$
 - c. The utterance time t_u is included in a time t', which is included in the time of John's running (which entails that the utterance time t_u is in the time of John's running).

From the example in (57) it becomes evident that our proposal of present-tense meaning, derives the correct semantics for mono-clausal present tense sentences. Moreover, and here we essentially build up on insights by Heim (1994); Altshuler (2016), this semantics predicts the facts observed in (53), as they interact differently with different embedding environments. To see this, let us first consider a context in which present tense morphology is embedded under a future-tensed matrix predicate (cf. (53a)).

From our discussion of the future-embedded past tensed sentence in (27), i.e., Alan will think everyone hid, we know that the shifter will does not carry a [uPAST] feature and that it must occur outside of the domain of Op-PAST as a result. In fact, we assume—similarly as we did for would (cf. discussion surrounding (21))—and in line with many others (e.g., Abusch, 1988; Ogihara, 1996; Condoravdi, 2002) that will is the tenseless future-shifting operator woll (cf. (58)) in its present-tensed form, meaning that it carries a [uPRES] feature. Consequently, it must be checked by Op-PRES. (58) $\llbracket \operatorname{woll} \rrbracket = \lambda P. \ \lambda t. \ \exists t'. \ t' > t \ \& \ P(t')$

Furthermore, we again follow Zeijlstra (2012) in that the covert operator carrying [iPRES] must c-command the highest instance of [uPRES] at the lowest position where this is syntactically and semantically possible (cf. Section 2). Consequently, *Op-PRES* must take scope over *will* in (53a), leading to the operator's being valued against t_u , and turning it into a purely absolute operator (as in (57)). Hence, in future-embedded environments, the dual effect of *Op-PRES* remains invisible:

- (59) John will say Mary is ill.
 - a. [$Op-PRES_{[iPRES]}$ [woll_[uPRES] [John say [$-s_{[uPRES]}$ [Mary be ill]]]]] $\exists t' \supseteq t_u \qquad \exists t^2 > t' \qquad \exists t^3 \supseteq t^2$
 - b. $\exists t' \supseteq t_u \& [\exists t^2 > t' \text{ say}(\text{John}, t^2, [\exists t^3 \supseteq t^2 \& \text{ be-ill}(\text{Mary}, t^3)])]$
 - c. John's saying happens strictly after the utterance time t_u and time of John's saying is included in the time of Mary's illness.

The dual nature of the present tense operator does reveal itself, however, in presentunder-past embeddings, where it explains the double-access reading observed in (cf. (53b)). Here, Zeijlstra's (2012) economy constraint places *Op-PRES* in the embedded clause, resulting in *Op-PRES*'s relative tense parameter's being valued against the evaluation time provided by the matrix past tense morpheme. As a result, our proposal, correctly, predicts presentunder-past embeddings to have d-a readings:

- (60) John said Mary is ill.
 - a. [$Op PAST_{[iPAST]}$ [$-ed_{[uPAST]}$] John say [$Op PRES_{[iPRES]}$ [$-s_{[uPRES]}$] $\exists t' < t_u$ $\exists t^2 \le t'$ $\exists t'' . [t'' \supseteq t^2 \& t'' \supseteq t_u]$ $\exists t^3 \supseteq t''$ Mary be ill]]]]]]
 - b. $\exists t' < t_u \& [\exists t^2 \le t' \& say(John, t^2, [\exists t''. [t'' \supseteq t^2 \& t'' \supseteq t_u] \& [\exists t^3 \supseteq t'' \& be-ill(Mary, t^3)]]]]$
 - c. John's saying happens strictly before the utterance time t_u and both the time of saying and the time of utterance are included in the time of Mary's illness.

In sum, our approach systematically assigns either a sim or a d-a reading to embedded present tense morphology, while keeping the intuitive meaning of unembedded present tense intact. It assigns embedded present tense a sim reading when the matrix clause is headed by an Op-PRES operator, i.e., in present or future embeddings, and it assigns present tense a d-a reading when it is embedded in an Op-PAST-headed clause.

Even though such a proposal makes the correct predictions, one might wonder why, at least in the case of matrix present tense, the time of utterance is introduced into the semantics twice, via two different mechanisms, i.e., once via being encoded in the semantics of Op-PRES and once as a default variable for the highest temporal argument slot. But, as said before, here we follow Heim (1994) and Altshuler (2016), who have provided various arguments for the inherent dual nature of present tense semantics.

4.2 Formal implementation

Along the lines of our presuppositional past tense proposal, we assume both Op-PRES and the present tense morpheme -s to be complex tense heads. The components and their functions are entirely parallel to those of the past tense proposal, with the exception of the presuppositions that the relevant partial identity functions contribute. Both of these, however, are directly derived from the quantificational proposal introduced in Section 4.1. As a result, the following denotation arises for the covert operator:

(61)

$$Op-PRES_{\langle st,st \rangle}$$

$$T-shift_{\langle i,\langle st,st \rangle\rangle}$$

$$Pres_{\langle i,i \rangle}$$

$$1_i$$

(62)
$$\llbracket Op\text{-}PRES \rrbracket^{g,t} = \lambda P : g(1) \supseteq t \& g(1) \supseteq t_u. \llbracket P \rrbracket^{g,g(1)}$$

Likewise, each present tense morpheme -s contributes the following semantics:

(63)

$$\operatorname{RI}_{\langle i,i\rangle}^{-S_i}$$

(64)
$$[\![-s]\!]^{g,t} = g(2) \supseteq t. g(2)$$

With these semantics in place, it can be easily shown that the proposal makes the correct predictions. Reconsider, for example, the mono-clausal present-tensed sentence *John is running*. With an LF akin to that (46), the following denotation is derived:

(65) John is running.

a.
$$[TP \ Op-PRES_{[iPRES]} \ [FinP \ -s_{[uPRES]} \ [VP \ John be running]]]$$

i. $[VP]^{g,t} = \lambda t. \ \lambda w. \ be-running(John, at t in w)$
b. $[FinP]^{g,t} = \lambda w: g(2) \supseteq t. \ be-running(John, at g(2) in w)$
iii. $[TP]^{g,t} = \lambda w: g(2) \supseteq g(1) \land [g(1) \supseteq t \land g(1) \supseteq t_u]. \ be-running(John, at g(2) in w)$

As before, since in this case $t = t_u$, *Op-PRES* generates an overlapping presupposition, and the sentence's denotation can be reduced to the following:

(66)
$$\llbracket \operatorname{TP} \rrbracket^{g,t} = \lambda w : g(2) \supseteq g(1) \land g(1) \supseteq t_u$$
. be-running(John, at $g(2)$ in w)

Correctly, these semantics predict that sentence (65) can only be felicitously uttered in situations in which John's running time includes the time of utterance.

Likewise, the distinctive readings for embedded present tense follow naturally from this proposal. To see this, consider first the case of future-embedded present tense, which crucially may receive a relative interpretation (cf. (59)). For the derivation of these semantics assume again, uncontroversially, that presuppositional *will* receives the denotation of *woll* (cf. (21)), but is syntactically restricted to present-tensed contexts via the feature [uPRES].

The semantics of a future-shifted present-tensed clause then emerge as follows (already collapsing the two presuppositions *Op-PRES* contributes since, again, it holds in this case that $t = t_u$):

- (67) John will say Mary is ill.
 - a. [$Op-PRES_{1|iPRES|}$ [woll_{2[uPRES]} [John say [$-s_{3[uPRES]}$ [Mary be ill]]]]
 - b. $\lambda w : g(3) \supseteq g(2) \land g(2) > g(1) \land g(1) \supseteq t_u$. say(John, be-ill(Mary, at g(3) in w), at g(2) in w)
 - c. John's saying happens strictly after the utterance time t_u and time of John's saying is included in the time of Mary's illness.

These semantics correctly predict that sentence (67) can be felicitously uttered in a scenario in which Mary is not ill at the time of utterance, but in which she is ill by the time of John's saying event, which lies in the future of the time of utterance. At the same time, it can also be felicitously uttered in a scenario in which Mary is already ill at the time of utterance and remains ill throughout, until the time of John's saying event.

Finally, we also correctly explain d-a readings. In such a case, the dual nature of the present-tense presupposition becomes visible and the presuppositional denotations of past and present tense combine in the following way:

- (68) John said Mary is ill.
 - a. [$Op-PAST_{[iPAST]}$ [$-ed_{[uPAST]}$ [John say [$Op-PRES_{[iPRES]}$ [$-s_{[uPRES]}$ [Mary be ill]]]]]]
 - b. $\lambda w : g(4) \supseteq g(3) \land [g(3) \supseteq g(2) \land g(3) \supseteq t_u] \land g(2) \le g(1) \land g(1) < t_u$. say(John, be-ill(Mary, at g(4) in w), at g(2) in w)
 - c. John's saying happens strictly before the utterance time t_u and both the time and the time of utterance are included in the time of Mary's illness.

5 Conclusion

In this paper, we provide a novel syntactic-semantic account for SoT, which does not rely on two truth-conditionally distinct LFs for the derivation of the sim and b-s reading—a standard assumption in the SoT literature that has recently been called into question by, e.g., Altshuler and Schwarzschild (2012); Altshuler (2016). At the same time, we explain the systematic availability of both a sim and a b-s reading for past-under-past embeddings. We propose to disentangle the different meaning components of past tense via outsourcing its absolute past meaning into a structurally high, covert past operator (Op-PAST) while encoding a relative non-future meaning into the past tense morpheme (-*ed*), which is syntactically dependent on the aforementioned operator. The two readings are thus licensed via the weak precedence relation past tense morphology semantically contributes. We show that this approach can deal with the same challenges as other SoT approaches and has certain additional advantages as well, such as retaining the one-to-one mapping between past tense form and past tense meaning. We furthermore demonstrate that the proposal is extendable to present tense without further complications. Here, too, we propose, that tense is made up of two semantically active components, i.e., a covert operator which introduces the 'real' present tense semantics and a relative component, which establishes inclusion relations between the relevant predicate times and the evaluation times. The crucial component of this proposal is that we argue, along with others such as Heim (1994); Altshuler (2016), that what has commonly been argued to be an exceptional reading of present tense, i.e., its d-a readings in present-underpast embeddings, should actually be part of the inherent meaning of past tense, for us of Op-PRES. In unembedded contexts, the evaluation time of this operator falls together with the utterance time, which is why, in these cases, the semantic dual nature remains invisible. Once embedded under past tense, the dual semantics of present tense reveal themselves and immediately explain the double-access readings of such utterances.

Lastly, the account proposed in this paper is built on a number of parameters (e.g. the nolater-than semantics of past tense morphemes, *Op-PAST* being a relative past operator, a.o.), which, taken together, yields our analysis of past-under-past embeddings. The existence of such parameters opens up a space for variation, which in principle should account for crosslinguistic differences attested with respect to SoT. A proper investigation of the space of variation in this domain is a subject for future research.

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